

On the origin of the galaxy luminosity function

James Binney

Theoretical Physics, Keble Road, Oxford OX1 3NP

ABSTRACT

Evidence is summarized which suggests that when a protogalaxy collapses, a fraction f of its gas fails to heat to the virial temperature, where f is large for haloes less massive than the value M^* associated with L^* galaxies. Stars and galaxies form only from the cool gas fraction. Hot gas is ejected from low-mass systems as in conventional semi-analytic models of galaxy formation. In high-mass systems it is retained but does not cool and form stars. Instead it builds up as a largely inert atmosphere, in which cooling is inhibited by an episodically active galactic nucleus. Cold gas frequently falls into galactic haloes. In the absence of a dense atmosphere of virial-temperature gas it builds up on nearly circular orbits and can be observed in the 21 cm line of HI. When there is a sufficiently dense hot atmosphere, cold infalling gas tends to be ablated and absorbed by the hot atmosphere before it can form stars. The picture nicely explains away the surfeit of high-luminosity galaxies that has recently plagued semi-analytic models galaxy formation, replacing them by systems of moderate luminosity from old stars and large X-ray luminosities from hot gas.

Key words: galaxies: formation

1 INTRODUCTION

The Cold Dark Matter theory of structure formation has enjoyed notable successes in recent years. Not only does it provide a unified interpretation of the cosmic microwave background (CMB) and galaxy clustering, but on smaller scales it has led to successful models of the Ly α forest and gravitational lensing by galaxies, both strong and weak. While controversy surrounds the compatibility of the CDM theory with the measured dark-matter densities deep within galaxies, it seems likely that problems in this area arise from our poor understanding of galaxy formation rather than pointing to genuine shortcomings in the CDM model (Binney 2003).

Since the CDM theory is a theory of the invisible, tests of the theory rely to a large extent on predictions of how dark matter affects the baryon content of the Universe. On large scales forces other than gravity can generally be neglected, so the physics is simple and reliable. On the smallest scales both strong and electromagnetic interactions between baryons are as important as gravitational interactions, so the physics is complex. We know that this physics somehow gives rise to stars and galaxies, but the details are obscure.

Given the importance of galaxy-formation theory for making observational predictions from the CDM model, strenuous efforts have been made to model galaxy formation in the presence of CDM. These efforts are strongly influenced by the papers of Rees & Ostriker (1977) and White & Rees (1978), which took it as axiomatic that gas that

falls into a gravitational potential well immediately shocks to the well's virial temperature. Galaxies were assumed to form as this rapidly heated gas slowly cooled. I argue here that this picture is wrong. In reality galaxies are formed from the the significant fraction of gas that fails to heat as it falls into the potential well, and that the fraction that immediately heats to the virial temperature is unable to cool subsequently. As the clustering hierarchy of the CDM model develops, the fraction of gas that heats to the virial temperature increases, so the efficiency of galaxy formation falls. The argument draws on recent developments in the study of 'cooling flows', simulations of baryonic infall (Birnboim & Dekel 2003; Katz et al. 2003), and semi-analytic galaxy-formation theory (Benson et al. 2003).

2 DOES GAS VIRIALIZE?

The influential papers of galaxy-formation theory by Rees & Ostriker (1977) and White & Rees (1978) considered it evident that when gas falls into a potential well, it would be shock heated to the well's virial temperature. In my thesis work (Binney 1977) I studied the shock heating of infalling gas in circumstances that maximized the chances of the gas shock heating: inspired by Zel'dovich's pancake theory of galaxy formation I considered the accumulation of gas in a sheet of uniform surface density following the collapse of an initially homogeneous spheroidal body of gas. Gas in the equatorial plane was stationary at all times but

increased in density as gas fell onto it from the polar directions with steadily increasing speed. As the speed of the infalling gas increased, the post-shock temperature of the infallen gas rose. In analytic work I compared the cooling time of the post-shock gas with the time required for infalling gas to travel a distance equal to the distance of the shock from the equatorial plane. This comparison showed that if the cooling rate was dominated by bremsstrahlung, the shock would break away from the equatorial plane only if the radius of the collapsing ellipsoid exceeded 30 kpc. I used one-dimensional hydrodynamical simulations to test the analytical work and found that it seriously underestimated the importance of cooling because (i) the infall velocity only gradually rises to the characteristic virial value, and (ii) even in a pure hydrogen-helium plasma, cooling at low temperatures greatly exceeds the bremsstrahlung rate. In a galaxy-sized collapse bremsstrahlung never dominates the cooling rate, and even for a cluster-sized collapse bremsstrahlung is important only when the last mass fraction falls in. Consequently, the fraction of gas that heats to the virial temperature is negligible in a galaxy-sized collapse and much less than unity in a cluster-sized one.

I considered the impact on the heated gas fraction of inhomogeneities in the infalling gas, and concluded that they were likely to favour cooling by increasing the surface density at which gas impacts the equatorial plane. Hence I concluded that essentially no gas would heat to the virial temperature when a galaxy-sized halo collapses, in flat contradiction to the fundamental premise of the influential paper of Rees & Ostriker (1977).

When CDM replaced neutrinos as the favoured dark matter component in the 1980s, it became necessary to revisit my 1977 study because CDM gives rise to smaller and cuspier potential wells, favouring cooling, while it enables one to lower the baryon density, which favours heating. Demoralized by the scant attention paid to my 1977 study I did not do so, but recently Birnboim & Dekel (2003) have done something similar. They have performed one-dimensional hydrodynamical simulations of baryonic infall into a spherical potential well, and concluded that “most galactic haloes that have collapsed and virialized by $z \sim 2$ did not produce a virial shock. Haloes less massive than $10^{11} M_{\odot}$ never produce a shock even if the gas has zero metallicity. If the metallicity is non-negligible (e.g., $Z \sim 0.05$) this lower bound to shock formation rises to $\sim 7 \times 10^{11} M_{\odot}$.” It seems that the bottom line has changed very little in 25 years.

Further support for my contention that infall is ineffective in heating gas to the virial temperature is provided by Katz et al. (2003). They used smooth-particle hydrodynamics (SPH) to follow the evolution of a mixture of CDM and baryons in cosmological clustering simulations. They measured the maximum temperature T_{\max} reached by each gas particle within a given halo, and found that at infall redshifts $z \gtrsim 1$ the distribution of T_{\max} is distinctly bimodal, with about equal masses associated with peaks centred on $\sim 3 \times 10^4$ K and the virial temperature. At smaller values of z , the gap in a histogram of T_{\max} values fills in, but the distribution of T_{\max} values remains extremely broad, so a great deal of matter continues to fall in without heating to near the virial temperature. The quantity of infalling gas diminishes strongly over time, so most gas falls in when the temperature distribution is strongly bimodal.

Future increases in the spatial resolution of the simulations is likely to increase the fraction of gas that falls in cold since increasing the resolution raises the density of the densest, fastest-cooling gas and thus makes it harder for gas to heat to the virial temperature.

3 FEEDBACK AND THE GALAXY LUMINOSITY FUNCTION

The clustering of CDM has been extensively simulated and the popular ‘semi-analytic model’ of galaxy formation has been used to associate with each dark-matter halo a galaxy of given luminosity and colours (Kauffmann, White & Guiderdoni, 1993; Lacey et al. 1993; Cole et al. 1994; Kauffmann et al. 1999; Somerville & Primack 1999; Cole et al. 2000; Benson et al. 2003). The algorithms employed in semi-analytic models start by assuming that each halo’s quota of baryons shock heats to the virial temperature and then cools on the timescale that follows from the density of the gas. As gas cools it forms a cold disk within which stars form at some rate, so the mass and age distribution of the stellar population of any halo is determined, and its luminosity and colours can be predicted. Cole et al. (2000) provide a lucid account of this very detailed work.

The mass function of dark-matter haloes $\Psi(M) = dN/dM$ is predicted by simulations of dark-matter clustering (Jenkins et al. 2001). It is quite different from the galaxy luminosity function $\Phi(L) = dN/dL$ in two respects: (i) while at the low- M end $\Psi(M)$ is rather close to a power law $\Psi(M) \propto M^{-\beta}$ with $\beta \sim 2.17$, the luminosity function of galaxies can be fitted by Schechter’s (1976) formula $\Phi(L) \propto L^{-\alpha} \exp(-L/L^*)$ with a flatter slope: $\alpha \sim 0.95$ (Cole et al. 2001; Kochanek et al. 2001). (ii) While both Ψ and Φ fall below these power laws at large values of their argument, the luminosity L^* of the break in $\Phi(L)$ corresponds to galactic masses that are $\gtrsim 100$ times smaller than the mass of the break in Ψ . Thus, if one predicted $\Phi(L)$ by converting $\Psi(M)$ using the mass-to-light ratio of a typical L^* galaxy, one would predict too many galaxies at both extremes of the luminosity scale.

Two mechanisms provide plausible explanations of the relative dearth of low-luminosity galaxies: upon reionization at $z_{\text{ion}} \sim 6$, the temperature of the baryons would have risen to $T \sim 2 \times 10^4$ K even before any shock heating. Gas at this temperature cannot be effectively trapped in a potential well with a peak circular velocity v_{\max} smaller than $\sim 35 \text{ km s}^{-1}$ (Efsthathiou 1992; Quinn Katz & Efsthathiou 1996; Thoul & Weinberg 1996). Since only the more massive haloes have larger circular speeds, the only low-mass haloes with stars will be those that formed before z_{ion} . This prediction chimes nicely with the observation that dwarf galaxies are overabundant in clusters of galaxies because on the average cluster galaxies formed before comparable field galaxies.

Another mechanism capable of explaining the dearth of low luminosity galaxies is feedback from supernovae: a burst of star formation is expected to initiate the formation of a galaxy. The massive stars in this burst will complete their lives and explode as core-collapse supernovae on a timescale that is short compared to the dynamical time of the embedding halo. The supernova blasts will heat surrounding gas to temperatures $\gtrsim 10^6$ K. If v_{\max} is smaller than $\sim 100 \text{ km s}^{-1}$,

the hot gas will stream outwards and further star formation may be effectively suppressed (Dekel & Silk 1986).

Benson et al (2003) have recently re-examined the fit to the galaxy luminosity function that one obtains by applying the semi-analytic model to the known mass function of dark-matter haloes. They conclude that with the relatively large baryon density that is now mandated by studies of large-scale structure, especially the CMB, the semi-analytic model cannot simultaneously fit both the low- and the high-luminosity end of $\Phi(L)$. The strength of feedback by supernovae is poorly constrained and may be treated as a free parameter. When strong feedback is chosen, the density of low-luminosity galaxies can be made sufficiently small. However, the baryons expelled from low-luminosity systems later fall into haloes of larger mass and make them more luminous. The consequence is that there are then too many high-luminosity galaxies.

4 COOLING FLOWS

We observe systems that contain gas at the virial temperature: X-ray observations long ago showed that nearly all clusters of galaxies and most luminous elliptical galaxies have such gas. Thus we are in a position to check observationally an important ingredient of the semi-analytic model of galaxy formation.

The cooling time of the gas in galaxy clusters and elliptical galaxies decreases as one approaches the centre, and in most systems the central value of the cooling time is much shorter than the Hubble time. This observation led to the expectation that gas in these systems was steadily forming stars as it cooled (Cowie & Binney 1977; Fabian & Nulsen 1977). From the radial surface-brightness profile of the X-rays and the assumption that the ‘cooling flow’ had reached a steady state, one can derive the rate of star formation as a function of radius (Nulsen 1986). Massive-star formation is certainly not taking place at the rate predicted by a Salpeter-like initial mass function (IMF), and formation of predominantly low-mass stars could also be excluded (Prestwich et al. 1997). Nor was cold gas present in the quantity required if star formation was somehow suppressed (Donahue et al. 2000; Edge 2001; Edge et al. 2002). Data from the Chandra and XMM-Newton satellites has recently shown that very little if any gas is cooling in clusters of galaxies, notwithstanding their short cooling times (Tamura et al. 2001; Peterson et al. 2002). Appropriate data are not yet available for individual elliptical galaxies, but the presumption must be that their smaller ‘cooling flows’ behave in a similar way. It is evident that the gas is being heated.

The details of how the gas is heated are controversial and irrelevant to the present discussion. What matters is that (a) very little if any gas is cooling to temperatures lower than $\sim 1/3$ that of the main body of gas, (b) any cold gas is confined to the very centre of the system (Edge et al. 2002), and (c) this gas is dusty and is quite likely material that has fallen in cold and is unconnected with the hot gas (Sparks et al. 1989).

Another important implication of the study of extended X-ray sources is that the gas observed in these systems is not heated to the virial temperature by gravitational shocking, but by supernovae and/or an active galactic nucleus (AGN).

This fact was first recognized by Kaiser (1991), who pointed out that in the contrary case not only would the number of bright X-ray sources at $z \sim 1$ be greater than observed, but the correlation between luminosity and temperature at the present epoch would be less steep than is observed (Kaiser 1986). Kaiser’s inference has been confirmed in many subsequent studies (e.g., Shimizu et al. 2003). Direct evidence for non-gravitational heating is provided by the large fraction ($\gtrsim 50$ percent) of the heavy elements in clusters of galaxies which are contained in the X-ray emitting gas but must have been synthesized within the galaxies.

5 CALLING A HALT TO STAR FORMATION

The study of ‘cooling flows’ teaches us that systems in which all gas is at the virial temperature do *not* form stars and do *not* accumulate cold gas from which stars could form at a later date. The evidence for cold infall suggests that star formation in such a system could be restarted if a quantity of cold gas fell in. An episode of cold infall will not necessarily lead to star formation, however, because a sufficiently dense hot atmosphere will ablate and reheat infalling gas before it can form stars. In fact, we can assume that cold gas enters the virialized system at a density that does not permit rapid star formation, since otherwise it would already have fragmented into stars. Hence to form stars it has to accumulate in the halo potential, probably on some approximately closed orbits. The extended HI disks that are frequently observed around late-type galaxies are regions where such accumulation of cold infalling material is taking place. A sufficiently dense, hot atmosphere will inhibit this accumulation by ablating and stripping the cold gas, both (i) as it falls towards the closed parking orbits, and (ii) within those orbits. It will be highly vulnerable to ablation in phase (i) because its surface density will be low, but stage (ii) can last longer. A credible *ab initio* calculation of the ablation rate is hard because it would require a quantitative understanding of the magnetized, turbulent boundary layer between the cold and hot gas, which differ by at least three orders of magnitude in density.

6 PUTTING IT ALL TOGETHER

The following scheme seems to account neatly for all the evidence summarized above. When a dark halo virializes, a fraction f of the progenitor’s gas remains at $T \lesssim 10^4$ K, while the remainder heats to the virial temperature. The fraction f decreases as the halo mass increases. If the halo is massive enough, the fraction f is retained as a disk in which star formation commences. The gravitationally heated fraction is further heated by dying stars and by any massive black hole that forms at the system’s nucleus. In a lower-mass halo this gas expands and flows out of the system. As we move up the sequence to larger masses, the temperature that must be reached to push the hot gas out increases, and at some mass M^* , which we must identify with that of L^* galaxies, the gas cannot be pushed completely out of the halo, although it can be pushed so high into the halo that it takes several gigayears to fall back once the rate of heating by core-collapse supernovae has moderated (D’Ercole et al

1989). Once the hot gas cannot escape, its density steadily increases as dying stars inject fresh hot gas. At some point it becomes dense enough to ablate and absorb any infalling cold material before it can give rise to significant star formation.

The density of virial-temperature gas increases rapidly with halo mass near M^* because both the fraction $1-f$ and the ability to retain supernova-heated gas increase with M .

Current semi-analytic models of galaxy formation form too many high-luminosity galaxies when appropriate feedback is used because they assume that gas heated to the virial temperature can cool and make stars. Once this error is corrected, the models will yield luminosity functions that cut off sharply above L^* . Instead the revised models will predict that high-mass haloes will contain large masses of X-ray emitting virialized gas, in agreement with observation.

7 CONCLUSIONS

Observations of cooling flows lead to the conclusion that virial-temperature gas cannot cool and give rise to star formation. The inability of hot gas to cool when supernova heating is effective is obvious. The continued inability of this gas to cool once the supernova heating fades has surprised many, but can be readily explained and was predicted (Tabor & Binney 1993; Binney & Tabor 1995). The key point is that any very cold gas that forms, does so in the immediate vicinity of the central black hole, and induces accretion that promptly reheats the gas, largely shutting off further accretion. The details of this chain of events are inadequately understood, but the prospects for elucidating them are good (Reynolds et al, 2001; Omma et al 03).

Since gas heated to the virial temperature cannot cool and form stars, galaxy formation would be impossible if Rees & Ostriker were correct in assuming that gas is heated to the virial temperature when a system virializes. Three different simulations argue to the contrary that a significant fraction of the gas never reaches the virial temperature. Galaxies form from this under-heated fraction. In lower-mass systems the heated fraction is largely ejected. Some of this subsequently finds its way into more massive haloes. These haloes heat a larger fraction of their progenitor's gas to the virial temperature and tend to retain both this gas and gas ejected by their stellar systems. Consequently, they develop dense atmospheres of virial-temperature gas. These atmospheres ablate any cold gas that falls into their haloes, so star formation ceases in these systems. Consequently, high-mass haloes are now associated with only modest luminosities from rather old stars and substantial masses of X-ray emitting virial-temperature gas.

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